## Chapter 2 - Functions and Transformations

A function is a relation that maps inputs to outputs.
$\llcorner$ The function has both $y$ and $x$ values
$\llcorner$ The $\boldsymbol{x}$ value imputed in the function is called the domain
$\llcorner\quad$ The $\boldsymbol{y}$ value output by the function is called the range
Composite functions are formed when you combined two or more functions, for example:

$$
f(x)=3 x+2 \quad g(x)=7-x
$$

Therefore, $f g(\boldsymbol{x})$ would be the function $g$ entered as an input of $\boldsymbol{x}$ in function $f$ and simplified

$$
f(x)=3(7-x)+2
$$

The function inverse is the reflection of the function in the line $\boldsymbol{y}=\boldsymbol{x}$ changing all $\boldsymbol{x}$ coordinates to $\boldsymbol{y}$ coordinates and $\boldsymbol{y}$ to $\boldsymbol{x}$, thus switching the range and domain of a function.

How to find the inverse function

Make $f(\boldsymbol{x})$ as $\boldsymbol{y}$ and then make $\boldsymbol{x}$ the subject of the equation then replace $\boldsymbol{y}$ as $\boldsymbol{x}$, for example:

$$
\begin{gathered}
f(x)=3 x+2 \\
y=3 x+2 \\
y-2=3 x \\
(y-2) / 3=x
\end{gathered}
$$

So the inverse of $f(x)$ is $(x-2) / 3$

## Transformations of the functions

$\llcorner$ For any function $f(\boldsymbol{x})$, the graph of $\boldsymbol{y}=f(\boldsymbol{x})+\boldsymbol{a}$ can be obtained from the graph of $\boldsymbol{y}=f(\boldsymbol{x})$ by translating it through a unit in the positive $\boldsymbol{y}$ direction.
$\llcorner$ For any function $f(\boldsymbol{x})$, the graph of $\boldsymbol{y}=f(\boldsymbol{x}-\boldsymbol{a})$ can be obtained from the graph of $\boldsymbol{y}=f(\boldsymbol{x})$ by translating it through a unit in the positive $\boldsymbol{x}$ direction.
$\llcorner$ For any function $f(\boldsymbol{x})$, the graph of $\boldsymbol{y}=f(\boldsymbol{x}-\boldsymbol{s})+\boldsymbol{t}$ can be obtained from the graph of $\boldsymbol{y}=\mathrm{f}(\boldsymbol{x})$ by translating it through $\boldsymbol{s}$ units in the positive $\boldsymbol{x}$ direction and $\boldsymbol{t}$ units in the positive $\boldsymbol{y}$ direction.
$\llcorner$ For any function $f(\boldsymbol{x})$, and any positive value of $\boldsymbol{a}$, the graph of $\boldsymbol{y}=\boldsymbol{a} f(\boldsymbol{x})$ can be obtained from the graph of $\boldsymbol{y}=\mathrm{f}(\boldsymbol{x})$ by a stretch of the scale factor $\boldsymbol{a}$ parallel to the $y$-axis
$\llcorner$ For any function $f(\boldsymbol{x})$, and any positive value of $\boldsymbol{a}$, the graph of $\boldsymbol{y}=f(\mathrm{ax})$ can be obtained from the graph of $\boldsymbol{y}=\mathrm{f}(\boldsymbol{x})$ by a stretch of scale factor 1 parallel to the $x$-axis.

